

Equations and Inequalities

In an equation, if $a = b$, then $b = a$. In an inequality, if $a < b$, then $b > a$.

Example: $7 = 2 + 5$ and $2 + 5 = 7$
 $2 + 8 > 7$
 but $7 < 2 + 8$

When graphing inequalities, it is often easier to visualize the solution when the variable is on the left side of the inequality symbol.

Example 2

Solve $3 \leq b - 1\frac{1}{3}$. Graph the solution on a number line.

$$3 \leq b - 1\frac{1}{3}$$

Write the inequality.

$$3 + 1\frac{1}{3} \leq b - 1\frac{1}{3} + 1\frac{1}{3}$$

Addition Property of Inequality

$$4\frac{1}{3} \leq b \text{ or } b \geq 4\frac{1}{3}$$

Simplify.

The solution is $b \geq 4\frac{1}{3}$.

Check $3 \leq b - \frac{1}{3}$

Write the inequality.

$$3 \stackrel{?}{\geq} 4\frac{1}{3} - 1\frac{1}{3}$$

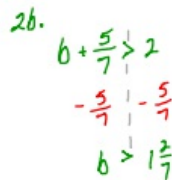
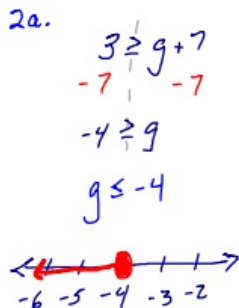
Replace b with $4\frac{1}{3}$.

$$3 \leq 3 \checkmark$$

The statement is true.

Graph the solution.

Since the inequality symbol is \geq , draw a closed dot at $4\frac{1}{3}$ with an arrow to the right.



Got It? Do these problems to find out.

Solve each equation. Graph the solution on a number line.

2a. $3 \geq g + 7$

2b. $b + \frac{5}{7} > 2$

Positive Number

The statement $c > 0$ means that c is a positive number.

Key Concept Multiplication and Division Properties

Words When you multiply or divide each side of an inequality by the same *positive* number, the inequality remains true.

Symbols For all numbers a , b , and c , where $c > 0$,

1. If $a < b$, then $ac < bc$ and $\frac{a}{c} < \frac{b}{c}$.

2. If $a > b$, then $ac > bc$ and $\frac{a}{c} > \frac{b}{c}$.

Examples $-6 < 10$ $20 > 16$

$$-6 \cdot 2 < 10 \cdot 2 \quad \frac{20}{4} > \frac{16}{4}$$

$$-12 < 20 \quad 5 > 4$$

These properties are also true for $a \leq b$ and $a \geq b$.

Some inequalities, like $4x > 8$, are solved by multiplication or division. You can multiply or divide each side of an inequality by a positive number and the inequality is still true.