

Solve Inequalities by Multiplication or Division

$$\left(\frac{5}{1}\right) \frac{x}{5} > 4(5)$$

$$x > 20$$

$$\frac{25}{5} > 4$$

$$5 > 4$$

✓

$$\left(\frac{5}{1}\right) \frac{x}{5} = 4(5)$$

$$x = 20$$

$$\frac{20}{5} = 4$$

$$4 = 4$$

✓

$$\frac{3x}{3} < \frac{12}{3}$$

$$x < 4$$

$$3(2) < 12$$

$$6 < 12$$

✓

$$\frac{3x}{3} = \frac{12}{3}$$

$$x = 4$$

$$3(4) = 12$$

$$12 = 12$$

✓

Solve Inequalities by Multiplication or Division

$$\begin{array}{l} 4 > 3 \\ 2 \cdot 4 > 2 \cdot 3 \\ 8 > 6 \end{array} \qquad \begin{array}{l} (-2)4 > 3(-2) \\ -8 < -6 \end{array} \qquad \begin{array}{l} \frac{10}{-5} < \frac{15}{-5} \\ -2 > -3 \end{array}$$

Lesson 6-7 - Solve Inequalities by Multiplication or Division

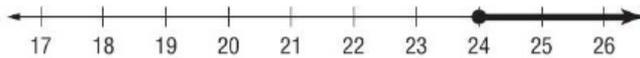
When you multiply or divide each side of an inequality by a positive number, the inequality remains true. However, when you multiply or divide each side of an inequality by a negative number, the direction of the inequality must be reversed for the inequality to remain true.

Example 1

Solve $\frac{t}{-6} \leq -4$. Then graph the solution set on a number line.

$$\begin{aligned} \frac{t}{-6} &\leq -4 && \text{Write the inequality.} \\ \frac{t}{-6}(-6) &\geq -4(-6) && \text{Multiply each side by } -6 \text{ and reverse the inequality symbol.} \\ t &\geq 24 && \text{Simplify.} \end{aligned}$$

To graph the solution, place a closed circle at 24 and draw a line and arrow to the right.



Example 2

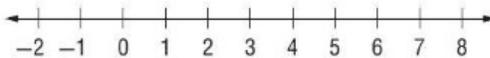
Solve $\frac{4}{5}x - 5 < 23$.

$$\begin{aligned} \frac{4}{5}x - 5 &< 23 && \text{Write the inequality.} \\ \frac{4}{5}x - 5 + 5 &< 23 + 5 && \text{Add 5 to each side.} \\ \frac{4}{5}x &< 28 && \text{Simplify.} \\ \left(\frac{5}{4}\right)\frac{4}{5}x &< \left(\frac{5}{4}\right)28 && \text{Multiply each side by } \frac{5}{4}. \\ x &< 35 && \text{Simplify.} \end{aligned}$$

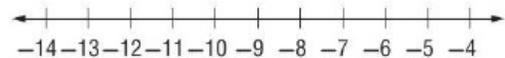
Exercises

Solve each inequality. Then graph the solution on a number line.

1. $3a > 12$



2. $6 \geq \frac{r}{-2}$



Solve each inequality. Check your solution.

3. $-3.1c + 2 \geq 2$

5. $-\frac{h}{5} - 6 < -10$

4. $13 > -\frac{2}{3}y - 3$

Handwritten work for problem 4:

$$\begin{aligned} 13 &> -\frac{2}{3}y - 3 \\ +3 & \quad +3 \\ 13 &> -\frac{2}{3}(-2) - 3 \\ 13 &> 14 - 3 \\ 13 &> 11 \end{aligned}$$

Handwritten work for problem 5:

$$\begin{aligned} -\frac{3}{2}(-16) &> -\frac{3}{2}\left(-\frac{2}{3}y\right) \\ -24 &< y \end{aligned}$$

Handwritten work for problem 6:

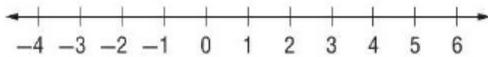
$$6a + 13 \leq 31$$

Lesson 7 Skills Practice

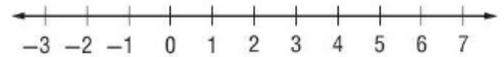
Solve Inequalities by Multiplication or Division

Solve each inequality. Graph the solution set on a number line.

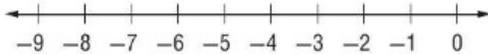
1. $3v > 12$



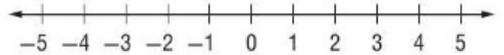
3. $-12 \leq -3g$



5. $\frac{a}{2} > -4$



7. $-14 \geq 7n$



Solve each inequality. Check your solution.

9. $3a + 6 < -10$

10. $\frac{b}{5} - 4 \geq -29$

13. $-6d + 7 \leq 1$

14. $\frac{z}{-8} - 5 < -3$

17. $3x + 2 < x - 6$

18. $y - 3 > 2y - 7$